

## METHODS FOR CLASSIFYING OBJECTS AND IDENTIFYING LATENT CLASSES

### RELATED APPLICATIONS

This application claims the priority of U.S. Application Serial No. 09/913,498,  
5 filed August 16, 2001, which is a Section 371 filing of International Application  
PCT/US01/03616, filed February 5, 2001, which in turn claims the benefit of the priority  
dates of earlier-filed provisional application Serial Nos. 60/180,282, filed February 4,  
2000, and 60/204,773, filed May 17, 2000, the disclosures of which are incorporated by  
reference herein.

#### 10 1. Field of the Invention

The present invention is directed to certain computational methods for classifying  
a plurality of objects or for identifying one or more latent classes among a plurality of  
objects. In particular, the present invention seeks to determine relationships between at  
15 least two sets of objects whereby one may determine the presence of latent classes of  
objects in one set or along one dimension, which latent classes may provide insight into  
possible distinctions, properties, or characteristics between objects in another set or along  
another dimension. More specifically, the present invention relates to a process for  
analyzing multivariate sets of data utilizing tools that combine, for example, aspects of  
20 fuzzy logic and statistics. The present invention finds a number of practical applications,  
including addressing a variety of informatics problems, such as those encountered in the  
field of biology. For example, the present invention enhances one's ability to  
comprehend data arising from gene expression experiments by grouping certain data

points into sensible clusters. Hence, the present method identifies latent (unobservable) properties of objects within a given sample or population, which properties are then useful to determine relationships and, potentially, classification schemes.

## 2. Background of the Invention

5       The present invention employs multidimensional, generalized, latent class structures in a statistical framework to identify and describe patterns. Examples of biological data amenable to analysis by this method can be found in two dimensional studies, for example, those involving a study of levels of gene expression, on the one hand, and the metastatic potential of tissue samples taken from different tissues, on  
10   another hand. In a manner analogous to a two-way ANOVA, statistically significant interactions between the two or more dimensions are identified. In the context of gene expression studies, these indicate pathways that are up- or down-regulated differently among different cells, tissues or experimental conditions. The present invention builds models for appropriate sets of data along a hierarchy of complexity.

15       In the context of gene expression studies, the method initially assumes that the underlying biological pathways may be on or off by degrees and that each gene's expression may be controlled by one or more pathways. For example, these pathways may be modeled to interact in a stochastic mixture. Based on residual analyses and other diagnostic modeling procedures (seeking ways to show that a chosen model does not fit  
20   the data in a reasonable fashion), or on external scientific information, initial models are enhanced. For example, stochastic mixture models may be enhanced by adding pathway interactions and physical mixing parameters, allowing one to evaluate contributions of

non-stochastic mixing. The present invention includes a feedback loop for building more complicated models to address such issues.

In addition, correlational information, such as pathology data concerning the observed mixing of cell types in a tissue sample, can be incorporated into the model. By  
5 establishing the effects of cellular contamination on the collected gene expression data and adjusting for these in a manner similar to ANCOVA prior to estimation of tumor-type differences, unwanted inter-person expression variability is substantially reduced. Examples that illustrate the ability of the present invention to decipher patterns of gene expression across microarrays (and to extract molecular fingerprints associated with  
10 particular tissue types) are given hereinafter.

Precise dissection of gene expression under a particular external influence or point in time can be achieved in high-throughput fashion by collecting data using cDNA microarray technology. Microarrays are microscope slides or membranes containing hundreds to tens of thousands of immobilized DNA samples. This array of cDNA-spots  
15 can then be probed with fluorescently labeled cDNAs, which are obtained by RT-PCR from total RNA pools corresponding to the test and reference biological sources. Following the hybridization step with two dye-tagged probes, the microarray is scanned to generate two images, each one corresponding to one of the dye "colors." Thus, the level of intensity at each particular point in each image corresponds to the amount of  
20 probe, tagged with the corresponding color dye, at that position. These images are typically captured as 16-bit TIFF-formatted files containing as many as 20 million-picture elements (pixels). The image pixels are converted to quantified gene expression data. Array image processing is employed to measure the intensity of the arrayed spots

and quantify their expression values. The resulting data consist of a number of measurements on spots related to specific genes.

Regardless of what algorithm is used to identify and quantify the image intensities related to gene expression, the resulting data must be modeled if one is to understand what biology underlies variation in gene expression over multiple microarray measurements. Such gene expression patterns can be quite complex. For example, existing knowledge has implicated numerous classes of genes and associated processes (angiogenesis, adhesion, invasion, growth and the like) in the development of tumor metastases.

The traditional method for predicting the clinical characteristics of a cancer involves obtaining a tissue sample from a subject; recording predictive parameters, specifically one or more morphometric descriptors or the results of a specific staining assay; and predicting the metastatic potential of the cancer by a statistical comparison of the recorded predictive parameters with corresponding parameters of a reference sample. Despite advances in our understanding of genetic events that underlie the development of cancers, the capacity to predict metastatic potential is limited, and the mechanisms underlying the process are poorly understood. At the present time, the traditional method in particular does not predict the potential for metastasis with sufficient certainty. Thus, the capacity to predict metastatic potential through an analysis of gene expression patterns taken from particular tumor specimens would be an important advance, potentially providing greater insight into the mechanisms responsible for this complex process and identifying new targets for therapeutic intervention. Conventional clustering

methods such as hierarchical clustering for example, are inadequate by themselves to resolve molecular fingerprints linked to colon cancer metastasis.

Indeed, others have come to a similar conclusion. For example, Tibshirani et al. have been working to develop a new technique based on principal components analysis, which they term "gene shaving," to enhance the results of hierarchical clustering. See, Tibshirani, R. et al., in "Clustering Methods for the Analysis of DNA Microarray Data," Preprint, International S-Plus User Conference, 1999: pp. 1-23. Tibshirani et al.'s intent was to discover a small set of genes whose expression across tissue samples best describes the directions of greatest observed variability over all the genes in the data set, without formally quantifying the grouped expression patterns themselves.

## 2.1 Fuzzy Logic and Statistical Methods

Fuzzy logic was proposed to be a superset of conventional (Boolean) logic, which has been extended to handle the concept of partial truth – that is, values between "completely true" and "completely false." It was introduced by Dr. Lotfi Zadeh of UC/Berkeley in the 1960's as a means to model the uncertainty of natural language. Fuzzy logic is implemented most commonly in control system design. Fuzzy logic-based systems are found in a rapidly growing number of consumer appliances (from dishwashers to video cameras), as well as in automobile engines and transmissions and industrial equipment. It is thought that the intuitive nature of the fuzzy-based system design saves engineers time and reduces costs by shortening product development cycles and making system maintenance and adjustments easier. The use of fuzzy logic for creating decision-support and expert systems in particular has grown in popularity among management and financial decision-modeling experts. Still others are putting it to work

in pattern recognition, economics, data analysis, and other areas that involve a high level of uncertainty, complexity, or nonlinearity. For example, Sony PalmTop uses a fuzzy logic decision tree algorithm to perform handwritten Kanji character recognition.

Semantically, the distinction between fuzzy logic and probability theory has to do with the difference between the notions of probability and a degree of membership. Probability statements are about the likelihoods of outcomes: an event either occurs or does not, and you can bet on it. But with fuzziness, one cannot say unequivocally whether an event occurred or not, and instead one tries to model the extent to which an event occurred. Although disagreements between statisticians and fuzzy-set theorists as to the consequences of this distinction have not been resolved to everyone's satisfaction, the developer of the present invention and his colleagues have demonstrated that fuzzy logic structures can be employed by statisticians when degrees of membership are treated as probabilities. In so doing it has been shown that the resulting mathematical forms, as employed by proponents of fuzzy-set theory, are poor ones to use in addressing most multidimensional applied problems. These findings are presented in Lazaridis, E.N., Discrimination and Classification Using Conditionally Independent Marginal Mixtures, in Department of Statistics. 1994, University of Chicago: Chicago, IL. p. 231; Lazaridis, E.N. Should we be fuzzy Bayesians? 1995. Orlando, FL: American Statistical Association; Lazaridis, E.N., A Bayesian evaluation of fuzzy logic in a classification problem. Communications in Statistics: Stochastic Models, 1999. 15(3), publications which are incorporated herein by way of reference.

Available statistical models for the analysis of multidimensional data also have substantial drawbacks. Typically, statisticians employ multivariate probability

distributions to model a multidimensional space. Such distributions are often difficult to employ or inadequate to reflect the underlying structures in the data. Alternatively, classification methods based on splines or classification trees are employed. Although they are easy to use, these also perform poorly in reflecting structure in commonly found  
5 non-linear spaces.

The present invention augments substantially, and is superior to, existing methodologies in current use (such as hierarchical clustering and principal components analyses) to analyze these kinds of data. In contrast to known techniques, the present invention seeks to explicitly model patterns, such as patterns of gene expression, across at  
10 least two dimensions, e.g., genes and tissue samples (or time), and to determine the probability that each gene or sample is a member of a latent class of genes or samples to which certain properties can be ascribed, e.g., the potential for metastasis.

The present invention provides a novel approach for classifying such data and for making intelligent deductions about the underlying biology. Whereas other available  
15 methods can perform only one-dimensional classification, the novel approach classifies these data along at least two-dimensions. Generally the novel method is designed to address multi-dimensional classification problems, where two or more dimensions are available for classification. This approach rests on the application of a novel combination of statistical and fuzzy logic methods.

Moreover, the present invention overcomes problems inherent to fuzzy logic and  
20 traditional statistical methods, combining elements of both to create more tractable model forms. The methods of the present invention offer significant improvements over

standard methods for the analysis of many kinds of data, including gene expression data from microarray experiments.

3. Summary of the Invention

Accordingly, it is an object of the present invention to provide a method of identifying one or more latent classes comprising: (a) providing one or more observations, each of which is associated with at least two members of a plurality of objects, which members can be allocated to at least two or more pre-existing categories; and (b) estimating one or more properties for latent classes from two or more distinguishable sets of latent classes, to which latent classes members of the plurality of objects may belong, which two or more distinguishable sets of latent classes correspond to two or more pre-existing categories to which members of the plurality of objects can be allocated. In a particular embodiment of the invention, the estimating step of step (b) optionally further comprises estimating one or more properties of at least one combination of at least two latent classes, which combination comprises at least one latent class from each of at least two of the two or more distinguishable sets of latent classes. In yet another preferred embodiment of the invention one or more properties of one or more latent classes or combinations thereof are specified and the estimating step of step (b) comprises estimating one or more unspecified properties of any latent classes or combinations thereof.

Moreover, in any of a variety of methods of practicing the present invention, for at least one latent class in the set of latent classes corresponding to the pre-existing category of one or more members of a plurality of objects, a probability is provided for assignment of the one or more members to the latent class. In this case, the estimating



step of step (b) comprises estimating one or more unspecified properties of any latent classes or combinations thereof.

In a specific method of identifying one or more latent classes, the present invention further comprises: (c) estimating, sequentially or substantially simultaneously with step (b), for each latent class in the set of latent classes corresponding to the pre-existing category of one or more members of a plurality of objects, a probability that the one or more members belong to the latent class. The present invention may further comprise: (d) classifying each member of the plurality of objects into one or more latent classes.

Consistent with the objectives of the present invention, a method is provided, as described above, in which the estimating step of step (b) comprises selecting a model appropriate for defining the one or more properties being estimated, which model comprises (i) a specified univariate or multivariate statistical distribution for each latent class and, optionally, for at least one combination of at least two latent classes, and (ii) an appropriate function relating the statistical distributions to the one or more observations. In such a method, the one or more observations may include one or more functional transformations of initial observations.

As an illustration of appropriate models for defining the one or more properties being estimated, a specific model is described, which can be characterized by a formula:

$$f(\tilde{Y}_{j_1, \dots, j_K}) I \left\{ j_k \in S_{km_{j_k}} \right\}_{k=1}^K \sim G \left[ h \left( k, j_k, \left\{ S_{km} \right\}_{m=1}^{M_k} \right)_{k=1}^K \right]$$

in which  $k \in \{1, \dots, K\}$  provides indexes of various directions in multidimensional space;  
 $j_k \in \{1, \dots, N_k\}$  identifies an object in a direction,  $k$ ;  $N_k$  represents the number of objects in  
the direction  $k$ ;  $\bar{Y}_{j_1, \dots, j_K}$  is a vector representation of one or more observations on a set of  
objects,  $\{j_1, \dots, j_K\}$ ;  $m \in \{1, \dots, M_k\}$  provides indexes of latent classes in the direction  $k$  with  
5  $M_k$  being the number of latent classes in the direction  $k$ ;  $S_{km}$  represents a latent class  $m$   
in the direction  $k$ ;  $G[\cdot]$  is a specified univariate or multivariate statistical distribution; and  
 $f(\cdot)$  and  $h(\cdot)$  are specified functions. Utilizing such an appropriate model, one or more  
parameters are specified for latent classes and, optionally, combinations thereof, which  
one or more parameters correspond to the one or more properties.

10 In an appropriate method of the present invention, the parameters are estimated by  
a procedure designed to estimate parameters of statistical distributions. Such a  
procedure, for example, might include but is not limited to a closed form solution, a  
Bayesian algorithm, an empirical Bayesian algorithm, a frequentist algorithm, a fuzzy set  
algorithm, or combinations thereof. Where the method of the invention utilizes a  
15 Bayesian algorithm, the algorithm may comprise, for instance, a Metropolis algorithm, a  
Gibbs algorithm, or a combination thereof. If a frequentist algorithm is preferred, such  
an algorithm may comprise an Expectation Maximization (EM) algorithm.

In another aspect of the invention, a method of classifying a plurality of objects is  
described, which method comprises: (a) providing one or more observations, each of  
20 which is associated with at least two members of a plurality of objects, which members  
can be allocated to at least two or more pre-existing categories; (b) providing one or more  
properties which completely specify all latent classes of interest and, optionally,

combinations thereof, from two or more distinguishable sets of latent classes, to which latent classes members of the plurality of objects may belong, which two or more distinguishable sets of latent classes correspond to two or more pre-existing categories to which members of the plurality of objects can be allocated; and (c) estimating for each  
5 latent class in the set of latent classes corresponding to the pre-existing category of one or more members of a plurality of objects, a probability that the one or more members belong to the latent class.

In yet another aspect of the invention a computer-implemented method of identifying one or more latent classes is provided, which method comprises: (a) receiving  
10 data corresponding to one or more observations or transformations thereof, each of which is associated with at least two members of a plurality of objects, which members can be allocated to at least two or more pre-existing categories; (b) setting a number of latent classes in each of two or more distinguishable sets of latent classes, to which latent classes members of the plurality of objects may belong, which two or more  
15 distinguishable sets of latent classes correspond to two or more pre-existing categories to which members of the plurality of objects can be allocated; (c) selecting a model appropriate for defining one or more properties to be estimated for each latent class, and optionally, combinations thereof, which model comprises (i) one or more parameters for each latent class and, optionally, combinations thereof, which one or more parameters  
20 correspond to the one or more properties, (ii) a specified univariate or multivariate statistical distribution for each latent class and, optionally, for at least one combination of at least two latent classes, which statistical distributions employ the parameters to characterize the distributional properties of each latent class and, optionally,

combinations thereof, and (iii) an appropriate function relating the statistical distributions to the one or more observations; (d) estimating the parameters by one or more procedures, sequentially or in parallel, which procedures are designed to estimate parameters of statistical distributions; (e) diagnosing whether the estimates obtained by application of the one or more procedures are reasonable in the context of the data being analyzed; (f) altering, as needed, the numbers of latent classes set in step (b) or the model of step (c) and repeating steps (d) and (e) until reasonable estimates are obtained; and (g) reporting summaries of the parameter estimates.

In a specific embodiment of the computer-implemented method of the invention, the estimating step of step (d) may comprise: (a) choosing one or more starting values for the parameters of the model; and (b) estimating the parameters by employing an EM algorithm. In particular, one may utilize a computer-implemented method that further comprises placing restrictions on the parameters of the model selected.

These and other aspects of the invention will become apparent to those of ordinary skill in the relevant art upon consideration of the descriptions provided herein, including the detailed descriptions of the preferred embodiments, which follow.

#### 4. Brief Description of the Drawings

FIG. 1 shows serum-stimulation patterns derived using the present invention, including median estimates and 95% confidence intervals from analysis of serum-stimulated fibroblasts, demonstrating both time-dependent increases and decreases in gene expression, as represented by positive (mostly red) and negative expression (mostly negative) patterns.

FIG. 2 displays comparative results from TaqMan and Microarray assays of the fibroblast data for 5 expressed genes.

FIG. 3 shows adjusted estimates of Mast and B4-2 expression derived by the present invention from the microarray data.

5        FIG. 4 illustrates effects of warm ischemia on mRNA populations. Different RNAs degrade with unique half-lives. As members of the initial RNA population become extinct, the relative levels of RNAs in the sample change. This is reflected in an apparent time-dependent pattern of expression when assayed using cDNA microarrays. mRNA levels from human colon mucosal samples subjected to 5, 10, 15, 30, 40, or 60 minutes of  
10        warm ischemia were measured relative to a reference cell line (KM12C) using cDNA microarrays containing 2,400 distinct elements. The data from 1420 elements is shown. Each row corresponds to a specific gene and each column a particular time point measurement. Red elements are expressed at an elevated level relative to the reference sample, green at a depressed level. (a) Expression levels following 5, 10, 15, 30, 40, or 60  
15        minutes of warm ischemia measured relative to a reference cell line (KM12C); in (b), the contrast and brightness have been adjusted to aid in visualization. Data in (c) can be used to infer the expression levels of each gene relative to its level at any other time point. In (c) data from times 5-15 min, A1, are averaged and displayed next to averaged data from 20-60 min, A2. In (d), the ratio of the averaged data from 5-15 min (A1)/ the averaged  
20        data from 20-60 min (A2) is displayed. Representations in (c) and (d) demonstrate that differences in gene expression do occur over the course of 60 min while EtBr-stained gel analyses and Northern analyses for GAPDH show no perceptible change over the same time course for normal mucosa (e) and tumor specimens (f).

FIG. 5 displays hierarchical clustering of time-course data for ischemic decay. (A) shows clustering results using the average of the three replicas for each time point. The dendrogram shows the time points related by progression. The 40 and 60 minute time points are most closely related to each other, and least related to the earliest time points. Similar results emerge when the measurements at each time point for each gene are compared to the measured value for that gene at (B) the 5 minute or (C) the 60 minute measurement. These results suggest a change in apparent expression level over time with an increasing deviation from the in-vivo measurement at greater ischemic times.

FIG. 6 shows ischemia patterns derived using the present invention, including median estimates and 95% confidence intervals from analysis of ischemia data at 6 time points (5 minutes to 1 hour), demonstrating various time-dependent increases and decreases in gene expression, as represented by positive (red) and negative (green) expression patterns.

FIG. 7 illustrates a CLONTECH filter.

FIG. 8 illustrates a portion of an NEN MICROMAX slide.

FIG. 9 illustrates a portion of an AFFYMETRIX chip.

FIG. 10 shows the estimated assignment of each of a set of tissues into each of a set of latent tissue classes estimated by the present invention.

FIG. 11 shows the interaction estimates ( $\gamma_{ml}$ ) between latent gene classes and latent tissue classes, as estimated by the present invention.

FIG. 12 shows a representative 2-D gel of proteins after exposure to peroxisome proliferators.

FIG. 13 shows phosphorylated and non-phosphorylated versions of a protein in a 2-D gel. .

FIG. 14 shows a flow diagram of a computer implemented process of the present invention.

5 FIG. 15 illustrates a process for Bayesian estimation employed by the present invention.

FIG. 16 illustrates multi-chain monitored algorithms employed by the present invention.

## 5. Detailed Description of the Preferred Embodiments

10 The present invention relates to methods that permit one to decipher patterns, relationships and other useful information from large amounts of data and making sensible connections between cause-effect events, which connections cannot be observed directly.

As mentioned above, a specific example arises in the context of predicting cancer  
15 metastatic potential through the molecular analysis of human cells or tumors. One goal of such an analysis might be to uncover patterns of gene expression that are observed from samples of cells or tissues, which patterns may portend metastatic potential of a particular tumor specimen or groups of tumor specimens. The present methods would be suitable, for example, for identifying in a genomic library one or more genes or sets of  
20 genes linked to metastatic properties of a cancer. It would also be beneficial in providing information to patients in the clinic of the relative metastatic potential of their tumor samples.

Cancer physiology can involve either the over-expression or repression of one or more gene products, or combinations thereof. The present invention can assess patterns of gene expression, which include both over- and under-expressed genes and which associates certain genes with properties of the cells or tissues that expressed (or under-  
5 expressed) said genes.

The present invention is useful, for example, in analyzing various forms of cancer, including colon cancer. It can be used to construct models for screening a wide variety of neoplastic diseases, including but not limited to solid tumors and hemopoietic cancers. Exemplary neoplastic diseases include carcinomas, such as adenocarcinomas  
10 and melanomas; mesodermal tumors, such as neuroblastomas and retinoblastomas; sarcomas, such as osteosarcomas, Ewing's sarcoma, and various leukemias and lymphomas. Of particular interest are adenocarcinomas of the breast, ovaries, colon, stomach, liver and lung.

Depending on the neoplastic disease, an appropriate patient sample is obtained by  
15 conventional methods. In the case of solid tumors, a tissue sample from the surgically removed tumor is obtained and prepared by conventional techniques for testing. In the case of lymphomas and leukemias, leukemic cells of blood or bone marrow or lymphoid tissues are obtained and appropriately prepared. Other patient or host samples, including urine, serum, sputum, cell extracts, etc. are also useful. As defined herein the term "host"  
20 denotes a mammal, preferably a human who may have a disease or be suspected of having a disease. Accordingly, the present invention is used to identify genes linked to the disease or stages thereof via analysis of cell or tissue samples collected from a



multiplicity of hosts, and to identify disease status in individuals suspected of having the disease.

In a preferred embodiment, the steps of the present method include organizing one or more measurements on each of the cell or tissue samples, or over a series of experimental or observational conditions, in an array of  $n$  dimensions ( $n$  being equal to or greater than two); allowing the different types of genes to form a first dimension and allowing the different types of cell or tissue samples to form a second dimension, associating each combination of gene and sample with one or more observed values (or observations); identifying latent classes of genes in the first dimension and latent classes of cell or tissue samples in the second dimension; establishing a relationship between the dimensions using a mathematical model; calculating the likelihood that each gene is a member of each latent class identified for the first dimension; and simultaneously or sequentially calculating a likelihood that each cell or tissue sample is a member of each latent class for the second dimension. This embodiment allows one to calculate the probabilities that the over- or under-expression of certain classes of genes are predictive of associated properties of specific tissue classes. For example, in the case of cancer metastatic potential, one is interested in identifying a class of genes that will allow one to differentiate between tumors with low vs. high metastatic potential. This then results in an estimated pattern of gene expression that, when compared against the gene expression of a previously unobserved cell or tissue sample, may be indicative of the capacity of the associated tumor to undergo metastasis (or the absence of such a capacity).

Representative cancers amenable to analysis using the methods of the present invention, include but are not limited to, leukemias such as acute leukemia; acute

lymphocytic leukemia; acute myelocytic leukemia; myeloblastic, promyelocytic, myelomonocytic, monocytic erythroleukemia chronic leukemia; chronic myelocytic (granulocytic) leukemia; chronic lymphocytic leukemia; Polycythemia vera; lymphoma; Hodgkin's disease; non-Hodgkin's disease; multiple myeloma; Waldenstrom's

5    macroglobulinemia; heavy chain disease; solid tumors sarcomas and carcinomas including fibrosarcoma; myxosarcoma; liposarcoma; chondrosarcoma; osteogenic sarcoma; chordoma; angiosarcoma; endotheliosarcoma; lymphangiosarcoma; Kaposi's sarcoma; lymphangioendotheliosarcoma; synovioma; mesothelioma; Ewing's tumor; leiomyosarcoma; rhabdomyosarcoma; colon carcinoma; pancreatic cancer; breast cancer;

10    ovarian cancer; prostate cancer; squamous cell carcinoma; basal cell carcinoma; adenocarcinoma; sweat gland carcinoma; sebaceous gland carcinoma; papillary carcinoma; papillary adenocarcinomas; cystadenocarcinoma; medullary carcinoma; bronchogenic carcinoma; renal cell carcinoma; hepatoma; bile duct carcinoma; choriocarcinoma; seminoma; embryonal carcinoma; Wilms' tumor; cervical cancer;

15    uterine cancer; testicular tumor; lung carcinoma; small cell lung carcinoma; bladder carcinoma; epithelial carcinoma; glioma; astrocytoma; ependymoma; craniopharyngioma; medulloblastoma; pinealoma; hemangioblastoma; acoustic neuroma; oligodendroglioma; meningioma; melanoma; neuroblastoma; retinoblastoma; and other types of tumors including virally induced cancers.

20            Another aspect of the present invention entails correlating protein expression and RNA expression to decipher patterns thereof. For example, one may be interested in patterns portending cancer metastasis, in establishing patterns associated with biological

pathways such as those associated with Signal Transducers and Activators of Transcription (STATs), or in defining phosphorylation signaling events.

The methods of the present invention also find utility in identifying disabilities, undesirable interactions between medications, co-morbidities, laboratory results and clinical characteristics linked to processes of aging, disease, cancer, diabetes, pregnancy, or other clinical or pathological conditions in humans. Preferably, the steps in such a method include describing in a matrix or array one or more measurements of said disabilities, medications, co-morbidities, laboratory results, clinical characteristics and so on, on each of a set of human subjects; allowing human subjects observed or treated under differing observational or experimental conditions to form the first dimension in the associated multidimensional space; allowing said disabilities, medications, co-morbidities, or laboratory results, etc. to form one or more additional dimensions; filling in the matrix or array with observations (e.g., symptoms, clinical observations, blood work, or the like); establishing a relationship between the dimensions using a mathematical model; identifying latent classes of human subjects in the first dimension, and latent classes of measurements in the second direction; and calculating the likelihood that each human subject is a member of each identified latent class for the first direction while also calculating, simultaneously or serially, the likelihood that each measurement is a member of each identified latent class in its associated dimension. In this manner, a relationship attributable to at least two latent classes, one each from the two dimensions described in this example, can be deciphered.

Other applications should be readily apparent to those skilled in the art. These applications may include but are not limited to studies of cellular processes associated

with cell metabolism, cellular damaging agents, biological pathways, protein expression, drug effects, and linkages between one or more expressed genes. Other applications may also include studies of processes of aging, physical processes in inorganic substances, chemical substances with pharmacological activity, and performance of financial vehicles  
5 such as stocks, groups of stocks, bonds, treasury bills and the like.

In a specific embodiment of the invention, the method can be reduced to the generation and analysis of cause-effect and/or stimulus-response profiles, preferably implemented by instructions executable by a computer (e.g., computer programs, software applications and the like).

10 The present invention can be applied to a combination of simultaneous mRNA and proteomic analysis of meticulously selected and acquired human tumor specimens to identify molecular patterns portending metastasis. Observations from such data gathering methods are used to initiate the present methods. Such observations may take the form of any measurable parameter and may include, but are not limited to, morphometric  
15 descriptors like the optical density of a measured object, object size, object shape, object color, and the like. Observations may also include the amount of DNA or RNA expressed, X-Y-Z coordinates in a multidimensional space, angular second moment, contrast, correlation, difference moment, inverse difference moment, sum average, sum variance, sum entropy, entropy, difference variance, difference entropy, maximal  
20 correlation coefficient, coefficient of variation, peak transition probability, diagonal variance, diagonal moment, second diagonal moment, product moment, triangular symmetry, sum entropy, standard deviation, and the like. One can also use cell classifications, e.g., 1 = Hypodiploid, 2 = Diploid, 3 = S-Phase, 5 = Tetraploid, and 6 =

Hyperploid, as initial observations or starting measurements, which may be further functionally transformed in one or more ways. Yet other forms of observations include blobness, perimeter, DNA index, maximum diameter, minimum diameter, elongation, run length, and any number of other measurable parameters known in the art.

5           In a preferred method of practicing the present invention, one or more measurements on selected objects, e.g., genes, cells, tissues and the like, are organized in a multidimensional array or matrix. The measurements or observations can be collected over a series of experimental or observational conditions. In the case of gene expression experiments, one allows genes to form a first dimension or one set of margins, and one  
10 allows cell or tissue samples to form a second dimension or second set of margins. The manner in which expression was measured can be permitted to form a third dimension or third set of margins. Indeed, one can allow other measurements to form one or more additional dimensions or sets of margins. The present method then seeks to make estimates of certain parameters or properties, which lead to the identification of latent  
15 classes to which members of the various objects may belong and which latent classes offer associations or relationships across two or more dimensions or margins. Accordingly, through the practice of the present invention, an association or relationship can be drawn between latent classes of genes on the one hand and latent classes of cell or tissue samples having varying degrees of propensity for cancer metastasis on the other  
20 hand. This association or relationship can then be exploited to a cancer patient's potential advantage by assessing the likelihood that a given tumor sample is, or has the capacity to be, in a stage of metastasis. In other words, one can determine the disease state of the subject cancer patient.

As a further illustration of the present invention, a study can be undertaken of effects of warm or cold ischemia and normal cell contamination on microarray or proteomics experiments. For example, the methods of the invention can be applied to studies of ischemic effects in human colonic mucosal samples. It is important, for instance, to evaluate the effects of *in vitro* and *in vivo* ischemia associated with the surgical and pathological procedures used to extirpate the tumor specimens and the contribution of normal infiltrating cells on the analysis of gene expression.

Thus, a preferred embodiment of this invention entails the determination of ischemia susceptible genes. In one experiment, data were collected regarding 1420 genes in a 2,400-element array, using cells subjected to ischemia lasting from 5 to 60 minutes. Because tissues historically collected and stored in tissues banks at many medical institutions were collected without regard to the length of time in which the tissues were subjected to ischemia, it is important that a method be established for adjusting data obtained from these tissues for potential "ischemic effects." Hence, the present invention contemplates the identification of genes or groups of genes, whose expression might be particularly susceptible to ischemic conditions. Hence, information obtained from samples concerning the expression levels of such susceptible genes or groups of genes can be corrected using the additional information and/or relationships uncovered by the methods of the present invention.

In yet another application of the present invention, a method is provided for the "re-analysis" of published data sets derived from various cell or tissue studies. For example, such data might include microarray data from time-course monitored serum-stimulated fibroblasts, or from human normal and cancerous colon tissues. The present

invention has been applied to analyze 8,613 different expressed genes in serum-stimulated fibroblasts, clearly discriminating genes over time with the identification of a refined set of patterns. It has also been applied to the analysis of almost 2,000 gene products to not only discriminate between normal and tumor tissues, but in addition, to  
5 identify molecular fingerprints of multiple kinds of tumor tissues. Tumors having different molecular expression patterns, which arise from different aberrations of the genetic code, manifest different characteristics that are important for arresting the progress of cancer and related anticancer therapies. Thus, the present invention contemplates methods of identifying and distinguishing among important tumor  
10 subclasses, by deciphering molecular fingerprints that allows one to discriminate among different tumor, cell, or tissue samples to identify those subclasses of high disease causing potential (e.g., those that might be associated with a high recovery rate or, conversely, with a high mortality rate).

A method is thus provided for identifying among a plurality of genes of known or  
15 unknown function those genes most likely linked to a condition of interest comprising:  
(a) providing a mathematical model that utilizes input data having two or more margins;  
(b) applying the mathematical model to the input data to obtain classification criteria that are based at least in part on information known about a condition of interest; and (c) selecting those genes that satisfy the classification criteria to identify those genes most  
20 likely linked to the condition of interest.

It is also an object of the present invention to provide a method of classifying two or more distinct objects comprising: (a) providing input data comprising attributes of each of the two or more distinct objects; (b) providing a starting model that is applied to

the input data and which comprises certain elements, including a desired number of latent classes, one or more marginal multivariate characteristics and, optionally, adjustable parameter restrictions; (c) estimating the starting model parameters; and (d) applying the starting model to the input data to obtain an output that can provide a tentative  
5 classification of the two or more distinct objects. In a specific embodiment of the invention, the method further comprises (d) optionally diagnosing the output to identify apparent discrepancies; (e) optionally refining one or more elements of the starting model and re-estimating the starting or refined model parameters, or a combination thereof. The method may include a further step (f) of reporting the output which includes the  
10 likelihood that certain members of the two or more distinct objects (e.g., certain genes and tissue samples) are related to one another (e.g., that over-expression of the certain genes indicates that the tissue sample has a high metastatic potential).

In another aspect of the invention, a method is provided for identifying one or more latent classes to which one or more members of a plurality of potentially distinct  
15 objects likely belongs comprising: (a) providing one or more attributes of each member of a plurality of objects; (b) assigning each of the one or more attributes to a region within a multidimensional matrix, in which a spatial relationship between the one or more attributes not occupying the same space in a given region can be mathematically described (e.g., by a vector), to generate raw input data; (c) applying a formula, which  
20 combines selected principles of statistical analysis and fuzzy logic, to process the raw input data to identify one or more latent classes to which the one or more members might belong, and further comprising determining the parameters of the spatial relationship which provide a strong likelihood that a given difference between one or more



characteristics attributable to the subject is sufficient to warrant further analysis (i.e., that a relationship might exist).

Once again, the present invention identifies potentially important patterns in multidimensional data not apprehended with conventional methods. As a general method of the present invention for classifying a plurality of objects, either simultaneously or sequentially, the following steps can be followed: one or more observations are collected on one or more sets of objects; the observations are ordered in a matrix or an array representing the multidimensional space for analysis; a model is chosen to represent the multivariate structure of the data. A preferred model has a mathematical representation chosen from among models of the form

$$f(\vec{Y}_{j_1, \dots, j_K}) | \{j_k \in S_{km_{j_k}}\}_{k=1}^K \sim G \left[ h \left( k, j_k, \{S_{km}\}_{m=1}^{M_k} \right)_{k=1}^K \right];$$

latent classes are identified along one or more of the constructed dimensions; the likelihood is calculated that each object of interest belongs to each of the identified latent classes along its specific dimension; objects are assigned among the identified latent classes along each dimension according to the estimated likelihoods. In this formula  $k \in \{1, \dots, K\}$  indexes the directions of the multidimensional space;  $j_k \in \{1, \dots, N_k\}$  identifies an object in direction  $k$ ;  $N_k$  is the number of objects in principal direction  $k$ ;  $\vec{Y}_{j_1, \dots, j_K}$  is a vector of one or more observations on a set of objects  $\{j_1, \dots, j_K\}$ ;  $m \in \{1, \dots, M_k\}$  indexes latent classes in direction  $k$  with  $M_k$  being the number of latent classes in direction  $k$ ;  $S_{km}$  is a latent class  $m$  in direction  $k$ ;  $G[\cdot]$  is a specified univariate or multivariate distribution; and  $f(\cdot)$  and  $h(\cdot)$  are specified functions.

In addition, in the context of microarray experimentation, models in the form, for example, of the family

$$\log(Y_{ij}) | i \in S_m, j \in G_l \sim N \left[ f(t_{il}, \alpha_{mi}, \beta_{lj}, \gamma_{ml}), \sigma^2 \right]$$

have been found useful in studies to identify one or more genes in molecular fingerprints linked to a cellular phenotype, to a biological pathway, to transcriptional effects of a drug, to metastasis potential of human colon cancers, and to differences between multiple types of tumors. In the above formula,  $N[\cdot]$  refers to a Gaussian distribution;  $S_m$  is a latent class  $m$  in the first dimension, referring to a category of cell or tissue samples;  $G_l$  is a latent class  $l$  in the second dimension, referring to a category of genes; and  $f(t_{il}, \alpha_{mi}, \beta_{lj}, \gamma_{ml})$  is a function of parameters related to a sample category ( $\alpha$ 's), gene category ( $\beta$ 's), sample by gene category interactions ( $\gamma$ 's), and gene-specific intensity expression intensity ( $t$ 's). These models provide the present invention with the capacity to assign probability statistics to the patterns or pathways to which genes are assigned. Thus, the present invention employs two-dimensional, generalized, latent class structures in a statistical framework to identify and describe patterns among genes (first dimension) and tissue sources (second dimension). In a manner analogous to two-way ANOVA, statistically significant interactions between the two dimensions are analyzed and reveal pathways that are up- or down-regulated differently among different microarray experiments.

The present invention is distinguished from conventional approaches used to explore microarray data in that the present invention uses flexible, non-parametric probability structures to identify and quantify data patterns. Non-probabilistic algorithms

estimate patterns based on relative distances of the expressed genes from one another in the multidimensional array space. Depending on what metric or space-exploring algorithm one chooses, one obtains very different results across methods, with no formal means for deciding among competing models. This dilemma is of especial concern in the context of gene discovery, where poor assignment of expressed genes with unknown function to the wrong patterns may lead to superfluous or misallocated laboratory experimentation. Formal statistical understandings of large gene sets are also necessary if microarray-like technologies are ever to mature beyond the exploratory laboratory research setting. For example, early detection of metastatic potential may ultimately require evaluation of the joint expression of hundreds of genes in order to predict disease status with high sensitivity and specificity. The expression pattern of any particular sample would need to be compared to and adjusted for possibly dozens of identifiable, highly multidimensional expression fingerprints. The present invention relates to the discovery that formal but flexible probabilistic models are natural and strong candidates for this kind of analysis, which has previously been unavailable.

Thus, the specific advantages of the present invention include the following: (1) it incorporates exploratory models, with intentionally weak structural assumptions so as not to impose artificial patterns on the data, making them very useful tools for complex data exploration; (2) it estimates broad expression patterns over genes and over cell or tissue samples, allowing one to quantitatively determine new biological knowledge; (3) it assigns to individual genes probabilities of membership in specific patterns, allowing one to quantify uncertainty associated with allocating elements among sets of interpretable categories; (4) it is used to conduct formal hypothesis testing; for example, one can

evaluate whether an identified gene pattern is significantly different from a null-hypothesis pattern; and (5) it incorporates complex model structures that can be used to exploit external biological knowledge. For example, prior knowledge about expressed genes known to be linked to P53 can be exploited to improve the performance of the present invention, by honing in on the pathways in which these genes reside.

The practical utility of this approach is illustrated by analyzing three sets of data:

(1) The first is data collected in an experiment on fibroblasts that are first serum deprived and then stimulated, to investigate growth-related changes in RNA products over time (see for example Iyer, V.R., et al., The transcriptional program in the response of human fibroblasts to serum [see comments]. Science, 1999. 283(5398): pp. 83-7, incorporated herein by reference); (2) The second represents data derived from the effect of ischemia on the fidelity of microarray expression measurements; (3) The third is a set of colon cancer and normal tissue data (e.g., Alon, U., et al., Broad patterns of gene expression revealed by clustering analysis of tumor and normal colon tissues probed by oligonucleotide arrays. Proc Natl Acad Sci U S A, 1999. 96(12): pp. 6745-50, incorporated herein by reference).

As a further illustration of the methods of the present invention, additional representative examples are provided, which examples should not be construed as limiting the invention in any way. Following examples of the present invention in the biological arena, examples of non-biological problems to which the present invention is immediately applicable are provided.

## 6. Examples

### 6.1 Growth-Related Changes In Gene Expression In Fibroblast Cells

In a time-course experiment on fibroblasts, cells are first serum deprived and then stimulated, to investigate growth-related changes in RNA products over time. Other sets are additionally treated with cycloheximide. Samples of untreated and treated  
5 cells are collected at 12 and 4 time points, respectively, as are samples of unsynchronized cells. Microarrays include 8,613 gene products but present analysis includes about 517 of these. Iyer et al. used a hierarchical clustering algorithm to identify 10 patterns of gene expression in a subset of 517 genes, which was filtered before application of the clustering algorithm on the basis of the existence of “significant” univariate observed  
10 variability or fold changes in gene expression over time.

The present invention estimates parameters of an intensity-modified homologue of Skene and White’s (1992) latent class model for repeated measurements experiments. In this example, the complete set of 8,613 gene products is analyzed over all the time points and experimental conditions, employing a normal error model on the  
15 log-transformed data, with mean conditional on latent gene class and time (plus experimental condition), with gene-specific intensity modifiers to represent the degree to which each gene is a good marker of its associated latent gene class. This approach uncovers about 9 time-correlated patterns. Genes have either decreased in expression (negative intensity modification parameters) or increased in expression (positive intensity  
20 modification parameters).

FIG. 1 presents both the estimated patterns and their inverses. In other words, red and green colors represent, respectively, higher or lower levels of expression

relative to untreated cells at time 0. A white background aids visualization; brighter colors represent greater relative deviation from baseline.

In addition, the invention adjusts for the data quality in the underlying microarray data. Specifically, an observation (one spot on one microarray slide) is treated as missing whenever the inter-pixel correlation between the two scans is less than 0.6. Thus, the invention accounts for and is unbiased by differential hybridization of samples. A consequence of this is that Pattern VIII is distinct from Pattern VI because of insufficient information at samples 1, and 9 through 13, as evidenced by a wide confidence interval ranging from very bright green (2.5 %-ile) to very bright red (97.5 %-ile). Probabilities of gene membership in these latent patterns for every gene in the data are also estimated by the model.

This example illustrates some additional advantages. Estimated time-course patterns are smoother than those resulting from hierarchical clustering analysis, even though no smoothness criterion is imposed by the chosen model. Although no assumptions are made regarding the correlations within treatment group across time, the estimates show expression patterns that are correlated with known stages of cellular growth and mitosis, indicating that our model is uncovering the underlying biology. No pre-filtering of genes is required by the new technique. Data quality issues are adjusted by using statistical approaches, to reduce the potential biases that can be introduced by experimental variability, especially at low spot intensities. Standard statistical approaches to diagnose lack-of-fit of the instant model to the data are also feasible.

The invention makes it possible to adjust for known issues with microarray estimation of true expression relative to Northern blot experiments. By way

of illustration the published TaqMan assay and microarray results of the above fibroblast data for 5 expressed genes are reproduced in FIG. 2. Although there is substantial correlation between the results, they are quite different. Specifically, the microarray data is overall more variable across the experiment, underestimates large changes in RNA expression, and suffers from edge effects. All three problems are illustrated by the Mast and B4-2 genes. For example, the TaqMan assay provides that there are substantial differences in expression between Mast and B4-2 from 4 hours on, at which time Mast is an order of magnitude more repressed than B4-2. Because the present invention pools information across gene products and microarray hybridizations, it uses biological correlations across measurements to reduce biases in particular observations. The present invention also adjusts for biases inherent to specific biological techniques.

FIG. 3 shows adjusted estimates of the present invention of Mast and B4-2 expression derived from the microarray data. This approach is easily adaptable to other situations, such as for example analyzing changes in expression of fibroblast and epithelial cells in response to selenomethionine, a compound known to decrease clinical risk of certain cancers in high-risk groups. Data from Northern blot and microarray data can be analyzed using the invention to verify and adjust expression quantitation.

To characterize and control the intrinsic variability associated with the microarray process, KM12 human colon cancer cell lines are used as a renewable source of control RNA. To estimate the number of repetitions required for consistent estimation of a single sample's gene expression pattern, replicate microarray analyses are tested. Initially, hybridization data from as many as 20 chips across different RNA and probe preparations are obtained, and across chip construction runs of the microarrayer (up to

100 slides are produced per run). The within-gene between-run variabilities are compared, and information obtained is used in refining the analysis. These analyses identify steps in the microarray process that are highly variable, and can be controlled through alterations in procedure. These variabilities provide an important benchmark for  
5 quality control.

## 6.2 Ischemic Effects On Fidelity Of Microarray Expression Measurements

The degradation of RNA in tissue samples following excision from the patient can have a significant effect on the expression measurements that are derived from microarray analysis. If RNA species degrade at different rates, the relative  
10 population frequency of a particular species will change over time. A microarray comparison of RNA levels between identical samples subjected to different ischemic times could lead one to the incorrect conclusion that some of the genes on the array are differentially expressed.

For example, consider a particular tissue type in which there are only two  
15 RNAs present, RNA A and RNA B, and that these RNAs are expressed at the same level in normal tissue. However, RNA A is stable while RNA B decays with a relatively short half-life. Now, as a reference sample an amount of RNA equivalent to 1000 molecules is extracted; that sample contains, on average, 500 molecules each of RNA A and RNA B. When a second RNA sample from the tissue is extracted at some later time the level of  
20 RNA B are fallen to 20% of its starting value. At this time, the total number of RNA A molecules is unchanged, but the number of RNA B molecules is only 1/5 of its starting value. Consequently, the ratio of RNA A and RNA B is changed. Specifically, the same total mass of RNA from this later sample – 1000 molecules – will consist of 5/6 of RNA



A (833 molecules) and 1/6 is RNA B. If this sample is compared to reference sample, it would appear that RNA A had been up-regulated by 1.7-fold and RNA B had been down-regulated by nearly 3-fold.

If one compares two different patient samples without prior knowledge of the RNA stabilities or of the ischemic time the samples were subjected to, one concludes that these RNA species are differentially expressed. This illustration suggests that the handling of patient samples is crucial for generating meaningful expression data using microarrays in order to avoid reaching spurious conclusions regarding expression levels.

In order to test this occurrence the RNA levels are measured in a patient-derived tissue sample following different periods of warm ischemia. The goal is to see if the observed RNA levels might mimic results that would be obtained from a differential expression experiment.

Normal colon tissue removed during a bowel resection is divided into small sections immediately following excision. Tissue segments of approximately equal size are placed into liquid nitrogen at 5, 10, 15, 20, 40, and 60 minutes following removal. Total RNA is extracted using Trizol and RNA samples are used for microarray expression analysis. Poly(A+) RNA is prepared from each using oligo(dT) coated Seradyne magnetic beads and labeled oligo(dT) primed first-strand cDNA probes are prepared by incorporation of Cy5-dUTP. A reference probe is prepared and labeled with Cy3-dUTP using an equal quantity of mRNA extracted from the KM12C cell line.

For each time point, labeled cDNA from the clinical sample and from the cell-line control are co-hybridized to a microarray containing at least 2,400 distinct elements. Hybridized arrays are washed and then imaged using the ScanArray 3000

confocal laser scanner. TIFF images produced are analyzed using TIGR Spotfinder and background-subtracted integrated intensities for each spot are recorded. For each experiment, signal intensities between the two fluorescent images are normalized by separately summing the intensities in each channel and scaling the Cy3 intensities so that the summed intensities for both channels are equal. This normalization approach relies on the assumption that the same total quantity of RNA is used for both the query and control samples.

For each of the approximately 2,400 arrayed genes, the natural logarithm of the ratio of Cy5/Cy3 background-subtracted intensities is determined and used for subsequent analysis. The prior art includes performing gene and time-point cluster analysis using the Cluster/TreeView hierarchical clustering package (see incorporated reference Eisen, M.B., et al., Cluster analysis and display of genome-wide expression patterns. Proc Natl Acad Sci U S A, 1998. 95(25): pp. 14863-8), which uses Pearson correlation coefficients as a measure of similarity and average-linkage clustering. Clustering results are displayed visually, with each experimental time-point represented by a column in the display and each gene by a separate row. Elements of the display in Fig 4 are colored to represent its mean-adjusted ratio value; red-colored and green-colored cells represent, respectively, higher and lower levels of expression relative to the test sample; relative expression is represented by the relative brightness of the signal.

Of the 2,400 genes in the arrays at least 2,114 provide useful data in at least one experiment. Analysis of the 1,420 genes that gave signals above background for all eighteen measurements is performed. A time course, with genes clustered by temporal expression pattern, is shown in FIG. 4. In each colored figure, the temporal

expression pattern of each gene is represented by a horizontal row; the expression patterns of all genes in a single experiment is represented by a column. Using this red/green display, it is difficult to visually assess relative changes in gene expression levels over time.

5                   FIG. 4(C), represents the gene expression levels averaged from 5-15 min next to those averaged from 20-60 min to demonstrate visible differences over time. These differences are further emphasized in FIG. 4(D) where the ratio of these averaged gene expression levels is displayed and any color other than black represents a change in expression over time. These alterations in gene expression linked to ischemia over the  
10                   course of 60 min are not visualized in the ethidium bromide gel analyses and/or Northern analyses for a single housekeeping gene (FIG. 4(E) and 4(F)). Of the genes analyzed 45.4% (644 of 1420) show an increase in expression, 28.2% (401) show a decrease, and the remainder (26.4%; 375 of 1420) show a more complex temporal pattern of expression.

15                   Analysis by the prior art Eisen clustering analysis does identify some relationships suggesting that the earlier time points cluster away from later time points (FIG. 5); however, unlike the present invention, the prior art method gives no indication as to the reason for the clustering.

                  Application of the time-course model using the present invention reveals  
20                   that there are 3 patterns in the ischemia data, as shown in FIG. 6. These three prevalent patterns account for 68.2%, 17.8% and 13.4% of the 1420 genes, respectively. Pattern I corresponds to an average change of 27% over 60 minutes from 5 minute baseline level of expression. 63.8% of the genes with at least 80% probability of membership in this

pattern show average increases in expression over 60 minutes (left panel). The remainder decrease on average (right panel). Pattern II genes show the least ischemia-related effects, demonstrating an average change of only 12% over 60 minutes. In contrast to pattern I, 67.5% of the genes with at least 80% probability of membership in this pattern are decreasing in expression on average over time (right panel). The remaining 32.5% in this pattern increase an average of 12% over 60 minutes. Finally, pattern III genes (13.4% of the sample) show the greatest sensitivity to ischemia, changing an average of 50% over 60 minutes, with about the same number increasing as are decreasing.

In all these patterns, the null hypothesis of no change is not rejected with small sample size at any of the first 4 time points, from 5 through 20 minutes. In patterns I and III especially, 40 and 60 minute time points are found to deviate significantly from the 5 minute expressions. This is evidenced in the figure by confidence intervals that do not contain the 0 change or 1.00 relative expression ratio (white or no color) for averaged samples 5 and 6.

It is obvious that the analysis of more data and the conduct of more refined time-course experiments according to the teachings of the present invention, will allow one skilled in the art to determine both what genes are most susceptible to the effects of ischemia, and to design a microarray test that will grade tissue samples according to extent of ischemic degradation. Such an approach is extremely useful in adjusting data derived from tissue bank samples.

Based on these data, a number of clear conclusions are drawn. First, temporal changes in gene expression levels do occur following tissue excision, with detectable changes after as little as 20 minutes. This observation is in conflict with the

conclusions one might draw regarding the “quality” of the RNA based on 18s and 28s bands seen on a gel (FIGS. 4E and 4F). Typically, stability of RNA is usually determined by the integrity of the 18s and 28s ribosomal bands on an agarose gel. The gel shows a good 18s:28s ratio for tissue RNA samples obtained at all time points, which suggests that the RNA is stable.

However, microarray analysis of the same RNA samples clearly shows that there is significant degradation of RNA over time during ischemia. Thus, using the 18s:28s ratios as a measure of RNA stability is misleading. Regardless of whether these changes occur due to actual cellular processes or if they are the result of RNA degradation during ischemia, they produce significant and fundamental changes in the relative representation of RNA species. Consequently RNA samples compared from the same patient sample held for different times at room temperature following excision will exhibit patterns of differential expression that may be confounded with research questions, regardless of actual patterns of gene expression *in vivo*. These results suggest that unless tissue samples are carefully handled and snap frozen in an expedient manner, expression measurements are likely to be highly suspect.

### 6.3 Molecular Fingerprints Of Colon Cancer And Normal Tissues

Colorectal cancer is a common, deadly disease with 129,400 new cases and 56,600 deaths projected for 1999 in the United States. While surgical resection of localized tumors may be curative, the vast majority of deaths are linked to the metastatic spread of tumor cells. Sporadic colorectal cancer is known to arise from an accumulation of multiple, sequential somatic genetic changes within a cell, each of which likely has complex effects on gene expression. This invention addresses the problem of identifying

molecular fingerprints relating to colorectal cancer metastasis as a means of substantially improving diagnostic and prognostic capacities, and potentially elucidating new mechanisms underlying the metastatic process.

Sporadic colon cancer is the result of multiple, sequential somatic genetic alterations, which likely affect numerous pathways. Early epidemiological studies predicted that at least 5-6 genetic events would be required to generate a colon cancer. It is now appreciated that somatic mutations in the APC gene are common to the vast majority of colorectal cancers. Its mutation is the first step towards carcinogenesis, a step that leads to a multitude of complex downstream pathway effects. Its alteration often leads to truncation of its product, with subsequent downstream effects on multiple APC partners including catenin, p130Cas, E-Cadherin, and T cell factor-4 (Tcf-4). More specifically, it has been determined that mutations in APC or in catenin increase the activity of the catenin/Tcf-4 complex, leading to overexpression of c-MYC and cyclin D1 with subsequent promotion of neoplastic growth. APC mutation can now be related to the downstream effects of c-MYC on gene transcription and translation. For example, recent studies have demonstrated that MYC activities are modulated by a network of bHLH-Zip proteins with MAX at the center of the network. Whereas MYC-MAX complexes activate transcription, MAD-MAX complexes repress transcription.

For this reason, mRNA/protein levels of critical genes may increase or decrease in response to specific upstream stimuli. Like APC mutation, mutation of RAS is also thought to be an early event with downstream effects on signaling pathways involving many partners including Raf, MEK, and MAPK. Recently, Ras has been implicated in the Myc pathway by the finding that Ras enhances the accumulation of Myc

activity by stabilizing a protein with an otherwise short half-life. Subsequent to APC and/or RAS mutations, genetic events associated with tumor progression are thought to include the alteration of genes such as DCC, DPC-4, and P53.

Each of these somatic genetic events burdens affected cells by triggering multiple downstream changes in gene transcription and translation, thereby increasing the capacity of the cell to progress and develop deadly metastatic potential. The challenge is to identify the critical components of each pathway affected by these genetic alterations and to characterize the network connections.

Metastasis is a common problem linked to the altered expression of numerous genes. Metastasis is thought to be an evolutionary process based on the generation of tumor cells, which have accumulated a defined set of biological capacities through mutational events. These capacities include the capacities to develop new blood vessels, to grow, to invade protective basement membranes, to detach, to clump and form emboli, to evade host immune systems, and to attach and grow at distant organ sites. Failure to develop one or more of these capacities results in the elimination of metastatic potential.

To date, numerous molecules have been implicated in models of metastatic progression. These include angiogenesis factors such as VEGF, invasive enzymes such as metalloproteinases, collagenases, and heparinases, adhesion molecules such as integrins, cadherins, catenins, and annexins, and cell surface glycoproteins like CEA. Interestingly, the majority of molecules linked to the metastatic cell represent a sometimes subtle, over- or under-expression, of what is already expressed by the normal cell.

The evolution of metastatic potential occurs within the primary tumor. The process is the result of linked, sequential mutational events, whereby numerous phenotypic traits must be altered in some orderly fashion. It is now widely accepted that malignant tumors contain heterogeneous sub-populations of cells with significant biologic differences. Whereas the majority of cells in the primary tumor may have the genetic expression patterns predisposing to metastasis, these traits alone may be insufficient to produce a metastatic cell. The capacity of a tumor to metastasize is attributed to smaller sub-populations of cells, pre-existing within the primary tumor, which have both the predisposing and essential traits permitting distant spread. This model may be an oversimplification, but it does describe why the metastatic process is considered inefficient, with less than 0.1% of the primary tumor cells being capable of distant spread. While essential traits may only be found in small portions of the primary tumor, we believe that the predisposing traits, which precede the development of essential traits, are present in the majority of the tumor and will be prevalent enough to target and decipher.

Current staging systems based on anatomic descriptions are inadequate to predict metastasis. There are several clinicopathologic staging systems currently in use which are based solely on anatomic descriptions of tumor and the degree of tumor spread. The oldest system, the Dukes' staging system, delineates tumors into four groups (A,B,C,D) based on histologic evidence of tumor progression. Dukes' A tumors are node negative and involve only the mucosal and submucosal layers of the bowel wall. Dukes' B tumors invade deeper into the bowel wall involving a portion of, or complete penetration through, the smooth muscle layer. Dukes' C tumors metastasize locally to



the draining regional lymph nodes and Dukes D tumors metastasize distantly to organs such as the liver and lungs.

Despite the relative effectiveness of current staging systems, they do not incorporate prognostic variables such as differentiation, lymphovascular invasion, or  
5 clinical complications such as tumor perforation or fistula formation. Moreover, no genetic pathway information is utilized. Even well-studied single genes, such as P53, have yet to gain clinical favor, presumably because of their inability to significantly improve upon the power of current staging systems.

With the introduction of high-throughput microarray and proteomic  
10 technologies, however, new staging systems may incorporate extensive molecular data that differentiate fingerprints for tumor diagnosis and behavior. One testable hypothesis is that some of these differential fingerprints are directly related to the phenotypic (histologic) differences among tumors that permit differential recognition by pathologists. Other fingerprints may provide powerful prognostic information, but result in no visible  
15 phenotypic differences. More precise molecular staging would assist clinicians in better identifying the subsets of patients who might benefit from a specific therapeutic intervention while at the same time providing insight into the mechanisms underpinning the metastatic process.

Microarray expression analysis is used to analyze differential gene  
20 expression patterns. For the general notion of gene expression analysis by using microarrays several well-known references exist in the art as enclosed herein by way of reference: The principles of such technologies are disclosed in U.S. Patent Nos. 5,556,752, 5,744,305, 5,837,832, 5,843,655, 5,874,21 and 5,849,486. Published

International (PCT) patent applications, such as WO 99/27137 and WO 99/10538, disclose additional information, all of which are incorporated by reference herein. Illustrations of a CLONTECH filter (FIG. 7), an NEN MICROMAX slide (FIG. 8) and an AFFYMETRIX chip (FIG. 9) are provided herewith.

5 Many different types of microarrays thus exist which are all equally suitable for use in the present invention. In what follows, the new method is used to analyze published data on colon cancer and adjacent normal tissues, to demonstrate the ability to simultaneously identify and quantify molecular fingerprints that differentiate cancer from normal tissues, as well as latent gene classes, as described *supra*.

10 The data consist of gene expressions in 40 tumor and 22 adjacent normal colon tissue samples, that are derived from a commercial Affymetrix oligonucleotide array complementary to over 6,500 genes.

The invention employs two-dimensional models with forms like  $\log(Y_{ij}) | i \in S_m, j \in G_l \sim N[t_{il} f(\alpha_{mi}, \beta_{lj}, \gamma_{ml}), \sigma^2]$ , where  $i$  and  $j$  index the expression data by gene and sample respectively,  $m$  and  $l$  index latent classes on the corresponding dimensions, the  $t$  refer to gene-specific intensity parameters, and various forms for the function  $f$  are chosen. The following analytic results are based on an additive form for  $f$ ,  $\alpha_{mi}, \beta_{lj}, \gamma_{ml}$ , that is, an ANOVA-like additive model is used for incorporating main effects and an interaction term for the latent class means.

20 In one example of the implementation of this invention, one uses a Bayesian approach to estimate the parameters employed in the above model. Using its complete conditional distributions in the presence of weak prior information, a modified

Metropolis algorithm can be employed to converge to draws from the posterior distribution of this model. No information about the known cancer classification of the tissues is provided to this model, since the objective is to illustrate the invention's ability to differentiate and quantify molecular fingerprints of differing tissue types.

5           As a result, evidence is obtained to support the existence of up to 5 latent tissue classes in these data. Two of these classes contain relatively large proportions of normal or cancer tissues. The estimated assignment of each tissue into each latent tissue class is given in FIG 10. Tissues are assigned based on having a greater than 80% estimated probability of membership in a particular class.

10           The present invention identifies prevalent tissue classes that consist primarily of normal or cancer tissues, in latent tissue classes I and II, respectively. This is confirmed by Fisher's exact tests indicating that latent tissue classes I and II discriminate between normal and cancer tissues ( $p < 0.0001$ ).

15           The latent grouping of normal and cancer tissues uncovered in analysis by the present invention results from gene expression patterns across tissue samples. As in the two analyses presented above, genes are estimated to belong to each of a set of latent gene classes. In this analysis, 10 latent gene classes are found, each of which corresponds to a set of genes that express similarly both within and across tissues. In other words, genes in a single gene class would all tend to be elevated in the same tissues,  
20           or alternatively, repressed in the same tissues.

          The interaction between latent gene classes and latent tissue classes, as shown in FIG. 11, illustrates the ability of certain gene classes to discriminate among the estimated tissue classes. For example, this figure demonstrates that expressed genes that

are primarily in latent gene class 7 are upregulated in most normal tissues relative to most cancer tissues in this data set; however, they are also highly upregulated in tissue classes III, IV and especially V, which have tumor as well as normal tissues. The latent tissue class III has many relative expression levels between those of tissue classes I and II, 5 implying that it may consist of earlier stage cancer tissues and adjacent normal tissues with pre-malignant changes in gene expression.

This analysis illustrates the potential complexity of a molecular fingerprint that can discriminate among potentially interesting tissue classes. For example, use of a single gene in latent gene class 7 is likely to result in less powerful discrimination among 10 tissue types than would the use of a few genes in each latent gene class.

Taken together, a set of genes extracted from each of the informative gene classes can be used to generate a practical indicator of a tissue's molecular fingerprint, which can be applied to a dedicated microarray chip. For example, a set of gene culled from gene classes 1, 4, and 7 can together better discriminate between normal and cancer 15 tissues than can any single gene or single gene class alone. The present analysis allows one to select this set of genes, by identifying the genes that have the highest estimated intensity within each gene class, and therefore, these genes would be most useful as markers of the associated latent gene classes.

With the caveat that looking at individual genes is insufficiently 20 informative to distinguish among tissue classes, a series of genes in each of the estimated latent gene classes are considered, and as a result interesting results are obtained. For example, IGF binding protein, proto-oncogene RET precursor, and EGFR are all in latent gene class 1, meaning that the expression of these genes is elevated in most tumor tissues

relative to normal. Similarly, latent gene class 4 contains genes relatively overexpressed in most tumor tissues that encode for transcription factors, DNA binding proteins, ribosomal proteins and ataxia-telangiectasia, all of which are linked to neoplastic processes. Muscle genes considered discriminating and perhaps related to the existence of more contaminating muscle tissue in the normal colon samples, are found in latent gene classes 3, 6, 7 and 9, all of which are upregulated in the normal tissues. These findings concur with the added value of differentiating between muscle genes that are differentially expressed between most normal and cancer tissues (latent gene classes 3 and 7) versus those that are upregulated in both tissue types (latent gene classes 6 and 9).

This example demonstrates that a prognostic fingerprint can be identified by the novel method to select patients with, for example, liver metastases who could be cured from a resection procedure. Liver resection is potentially curative in up to 30% of patients selected, based on the number of colorectal liver metastases being <4, the location being generally unilobar, and the absence of porta hepatis lymphadenopathy. Despite being carefully selected for resection, there is currently no way to identify which 30% of the resected patients will be cured.

#### 6.4 Deciphering Comprehensive Proteomics Data

“Proteomics” is a recently coined term to denote the use of quantitative protein level measurements of gene expression to characterize biological processes and decipher the mechanisms of gene expression control. While gene expression may be directly linked to mRNA levels within the cell, it is not always the case that mRNA levels predict protein levels. In fact, it has been reported that protein and mRNA abundances may correlate poorly, with a correlation coefficient as low as 0.48, secondary to mechanisms

of post-transcriptional and post-translational modification. For this reason, the comprehensive evaluation of protein expression may be equally as important as the evaluation of mRNA expression.

Proteomics analysis is performed by combining 2D-gel electrophoresis (2D-GE),  
5 to separate and quantify protein levels, with two forms of mass spectroscopy to identify  
selected proteins of interest within the 2D gel. 2D-GE is the highest resolution analytical  
procedure for routine global analysis of proteins currently available, and it is now feasible  
to do large-scale quantitative protein mapping studies, albeit in only a few specially  
equipped laboratories worldwide. A number of non-quantitative or semi-quantitative  
10 2DE studies have been done to attempt to find exploitable differences between normal  
and tumor cells, and to develop databases of the protein composition of tissues including  
liver, brain, heart, keratinocytes, and blood proteins, among others. 2D maps of human  
plasma, urine, saliva, milk, semen, human lymphocyte proteins, human lens, and proteins  
of rat tissues are now available.

15 The principles of 2-D gel analysis of proteins are well established, e.g., Anderson,  
N.L. and N.G. Anderson, Analytical techniques for cell fractions. XXII. Two-  
dimensional analysis of serum and tissue proteins: multiple gradient-slab gel  
electrophoresis. Anal Biochem, 1978. 85(2): pp. 341-54; Anderson, N.G. and N.L.  
Anderson, Analytical techniques for cell fractions. XXI. Two-dimensional analysis of  
20 serum and tissue proteins: multiple isoelectric focusing. Anal Biochem, 1978. 85(2): pp.  
331-40.

2-D gel databases of proteins are commercially available from specialized  
companies, e.g., Large Scale Biology (LSB). LSB's Molecular Effects of Drugs™

(MED™) and Molecular Anatomy and Pathology™ (MAP™) databases contain more than 10 million protein abundance measurements. The MED™ database, for example, already contains 2-D gel information characterizing the effects of almost 100 chemical agents (mostly pharmaceuticals) on the protein expression pattern of rodent liver *in vivo*,  
5 and allows a molecular approach to the investigation of toxic and therapeutic mechanisms. The MED™ database is currently being expanded to include proteome analyses of more than 50 different human tissues. These databases provide master gels which are useful in the identification of proteins from unknown tumor specimens through gel matching techniques.

10 The LSB Kepler system involves an extensive two-dimensional mathematical filter that removes background, deconvolves each protein spot into one or more Gaussian peaks, and calculates the volumes under each peak (representing protein quantity). A multiple montage program allows the comparable areas of a series of up to 1,000 gels to be displayed and inter-compared visually to check on pattern matching. In matching  
15 individual gels to the chosen master 2-D pattern, a series of about 50 proteins is matched by an experienced operator working with a montage of all the 2-D patterns in the experiment. See, FIG 12 for a representative 2-D gel of proteins after exposure to peroxisome proliferators. As phosphorylated and un-phosphorylated versions of a protein occur at different locations on a 2-D gel, differential quantitation of the different  
20 forms is further assessed (FIG. 13). Subsequently, an automatic program is used to match additional 600-1000 spots to the master pattern using as a basis of the landmark data entered by the operator. A 2D-GE analysis of an individual tumor results in a protein molecular fingerprint which is directly compared to that of numerous other tumors.

Analysis of complex quantitative differences among a series of protein expression patterns can be performed using the present invention. A series of treated or diseased samples can be compared quantitatively, and abundance ratios (treated or diseased divided by normal control values) can be calculated for each protein spot. Subsequently, the present invention can be used to identify molecular fingerprints of proteins that distinguish among classes of samples. This is done by employing protein expression measurements in the place of gene expression measurements as had been employed in the previous illustration of application of this invention.

#### 6.5 Deciphering Pathways Related To A Particular Gene

P53, a tumor suppressor gene, is the most commonly mutated gene in human cancer, being mutated in up to 80% of colorectal cancer, and is likely involved more in tumor progression than initiation. The majority of the mutations are point mutations, which occur in codons 5-8, and result in single amino acid changes in the protein. Human cancers frequently contain an allelic deletion of the P53 gene, a deletion which is found in up to 70% of colon cancers. In addition, P53 has been found to contain germline mutations. In each of these cases, a somatic mutation of the remaining normal P53 allele may lead to sporadic cancer, as a result of altered or absent P53 protein activity.

The P53 protein is involved in cell cycle checkpoints in both G1 and G2. When DNA damage occurs, P53 levels increase, at least in part, because of stabilization of the existing protein by phosphorylation. Active P53 then induces one or more of the following events: cell cycle arrest, DNA repair, and apoptosis. In addition, evidence shows that there may be a gain of function in mutant P53, likely affecting downstream



gene expression. Analysis of DNA binding sites for P53 suggest that there may be a hundred or more genes, as yet unknown, which are regulated by P53.

For a general information regarding p53 and cancer oncogenes, the reader is referred to U.S. Patent Nos. 5,620,848, 5,527,676, 5,998,136 5,983,211, 5,747,469, and  
5 references therein, all of which are incorporated herein by reference.

Elucidation of the downstream effects of mutant P53 in cells will aid in the identification of possible targets for drug discovery. Metastatic tumors frequently harbor mutated P53 and gene expression patterns identified in cell lines with experimentally induced mutant P53 are comparable with human tumors known to contain mutant P53.  
10 These patterns are useful to decipher metastasis-specific gene expression patterns by identifying P53 linked gene expression patterns, or portions thereof, in tumors with documented metastatic behavior.

The gene expression patterns are produced by the overexpression of wild-type P53 by using human colon cancer cells with a wild-type, endogenous P53 (HCT 116)  
15 transfected with the V138 temperature sensitive mutant. At 32°C the mutant P53 does not disrupt wild type (wt) P53, thus MDM2 and p21 WAF are induced. At 39°C degrees, the mutant P53 disrupts wtP53 and results in inactivation of MDM2 and p21WAF. For additional background information, please refer to U.S. Patent Nos. 5,807,692; 5,858,976; 5,770,377; 5,756,455; 5,721,340; 5,708,136; 5,702,908; 5,702,903; 5,693,533;  
20 and 5,550,023, which are incorporated herein by reference.

As there is a large induction of MDM2 and P21WAF1, one can use this information to validate the microarray analysis, because both genes are represented in the available array. Thus our approach is valid and is readily adaptable to the exploitation of

publicly available data concerning the analysis of cells transiently transfected with wild-type P53. An analysis of as many as 7,202 transcripts yields at least 14 that are over-expressed at levels 10-fold greater than controls. By using microarray analysis setting appropriate parameters with considerably larger gene sets, more genes are likely to be  
5 obtained.

In addition to the instant V138 transfectants at 39°C as a model, other models of a cancer cell are equally suitable, e.g., transfected HCT 116 cells with a construct that expresses HPV E6, a protein known to target endogenous P53 for degradation. Critical differences in gene expression patterns between cell lines with over-expressed P53, wild-type P53, and suppressed endogenous P53, are thus addressable using either microarray  
10 or proteomic analyses. The patterns derived from these analyses are then compared with those from panels of cell lines with known P53 mutation (e.g., SW480, DLD-1 and the like) or wild-type P53 (LS180, HCT116 and the like) to determine their capacity to model P53 mutation in human colon cancer cells. It would be apparent to one skilled in  
15 the art whether these patterns are applicable in human tumors specifically harboring a mutant P53 gene versus those found to be wild-type for P53. And finally, these patterns induced by P53 mutation are directly comparable with gene expression patterns produced by tumors known to be metastatic, to determine if strong correlations or shared gene expression patterns exist.

#### 20        6.6    Characterizing A Drug Effect

Human hepatoma cell lines, Hep3B and HepG2, are obtained from American Type Culture Collection (Rockville, Md.). Cells are grown in Eagle minimal essential medium (MEM) supplemented with 10% fetal bovine serum. Freshly confluent

monolayers are washed twice with MEM and then incubated with fresh medium for 24 h in the presence of actinomycin D, a known inhibitor of transcription or in the presence of gemfibrozil, as an inducer of certain genes expression. Cell viability is routinely monitored by trypan blue exclusion and lactate dehydrogenase leakage.

5 Cellular mRNA is then isolated from HepG2 or Hep3B cells and hybridized with microarray. Differential expression is analyzed and data as a comparison template is fed into a computer. A new drug with unknown function is then assayed and is analyzed by comparison with set templates. The effect(s) produced by any other drug on the levels of expression of a given gene or cluster of genes can be determined similarly.

10 Drugs often have side effects that are in part due to the lack of target specificity. However, standard *in vitro* assay often misses the information on the specificity of a compound. In contrast, a genome reporter matrix reveals the spectrum of other genes in the genome also affected by the test compound. In considering two different compounds both of which induce the gene of interest, if one compound affects the expression of only  
15 10 other genes and a second compound affects the expression of 100 or more other genes, the first compound is, *a priori*, more likely to have fewer side effects. Because the identities of the primary genes of interest are known or determinable, information on other affected genes will be informative as to the nature of the side effect or genetic linkage to the first set of genes. A panel of genes can be used to test derivatives or  
20 analogs of the lead compound to determine which of the derivatives or analogs have greater specificity than the first drug or compound.

Alternatively, a test compound may not affect the response of a cell in an *in vitro* assay or may not affect the expression of a gene. In the traditional drug discovery, a

compound that does not display any activity will not provide any useful information. However, a compound having any significant effect on a biological process generally has some consequence on gene expression pattern. A genome reporter matrix can thus provide two different kinds of information for most compounds. In some cases, the identity of reporter genes affected by the inhibitor evidences to how the inhibitor functions.

For example, a compound that induces a cAMP-dependent promoter in yeast may affect the activity of the Ras pathway. Even where the compound affects the expression of a set of genes that do not evidence the action of the compound, the matrix provides a comprehensive assessment of the action of the compound that can be stored in a database for later analyses. A library of such response profiles can be established. For example, if the database reveals that compound X alters the expression of gene Y, and an article is published reporting that the expression of gene Y is sensitive to, for example, the inositol phosphate signaling pathway, then compound X is a candidate for modulating the inositol phosphate signaling pathway.

In effect the genome reporter matrix will readily provide information on a gene in relation to a compound that may already have been found to affect the expression of that gene. This tool dramatically shortens the research and discovery phase of drug development and more effectively realizes the value of the publicly available research databases on all genes.

#### 6.7 Financial Performance Of Investments (e.g., Stocks And Bonds)

Investors seek the highest possible investment return with minimal risk. Heavy investments in common stock produces high returns, for example, but these returns are

volatile, and losses due to stock volatility may severely impact the financial gain. It is difficult, however, to determine what mix of asset classes (what mix of certain stocks, for example) and in what proportion may produce the best results at an acceptable level of risk.

5           Various methods are currently used by financial managers of stocks in an attempt to maximize return. For example, one such method of solving the problem of maximizing return involves developing the asset allocation likely to produce the highest return at a given level of performance volatility. This method, however, is not a specific solution and therefore may not produce the best results for a given investor.

10           Another approach might be to develop the asset allocation that, within a stipulated time horizon at the calculated contribution level, will lead to an acceptable probability of achieving a selected funded ratio of assets to liabilities. Despite existing financial and mathematical model the risks are still real and in some cases are not acceptable.

15           The present invention provides a novel approach for managing risks of financial investments. The disclosed model, as described in detail in relation to identification of genetic linkage to a disease, is easily adaptable within the conditions of a financial market. By setting membership rules based on one or more measurements of stock performance one can easily identify or predict the members of latent classes.

20           Throughout this application, various publications and patents have been referenced. The disclosures in these publications or patents or references therein are incorporated herein by reference.

#### 6.8 Computer Implemented Process

FIG. 14 provides a flow diagram for a computer implemented process of the present invention. Also, FIG. 15 illustrates a process for Bayesian estimation as utilized by the present invention, and FIG. 16 illustrates the use of multichain monitored  
5 algorithms useful for developing solutions.

Although the foregoing invention has been described in some detail by way of illustration and example for purposes of clarity of understanding, it will be readily apparent to those of ordinary skill in the art in light of the teachings of this invention that certain changes and modifications may be made thereto without deviating from the spirit  
10 or scope of the present invention. Hence, no limitations on the scope of the invention should be implied by the specific embodiments chosen to illustrate the invention.